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GEOMETRIC METHODS
IN DYNAMICS (II)

VOLUME IN HONOR OF JACOB PALIS

edited by

Wellington de Melo

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GEOMETRIC METHODS IN DYNAMICS (II)

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Abstract. — This is the second of two volumes collecting original research articles, on several aspects of dynamics, mostly by participants in the International Conference on Dynamical Systems held at IMPA (Rio de Janeiro), in July 2000, to celebrate Jacob Palis' 60th birthday.

Résumé (Méthodes géométriques en dynamique (II). Volume en l'honneur de Jacob Palis)

Ceci est le second de deux volumes regroupant des articles originaux de recherche concernant des aspects variés de la théorie des systèmes dynamiques, écrits par certains des participants à la Conférence Internationale sur les Systèmes Dynamiques qui s'est tenue à l'IMPA (Rio de Janeiro), en juillet 2000 pour commémorer le 60^e anniversaire de Jacob Palis.

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